

# Heterogeneous Relaxation Dynamics in Amorphous Materials under Cyclic Loading

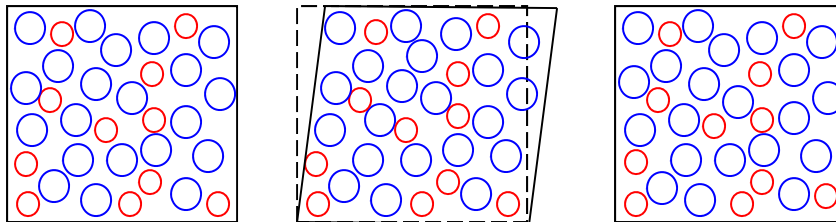
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Movies, preprints @ <http://www.egr.msu.edu/~priezjev>

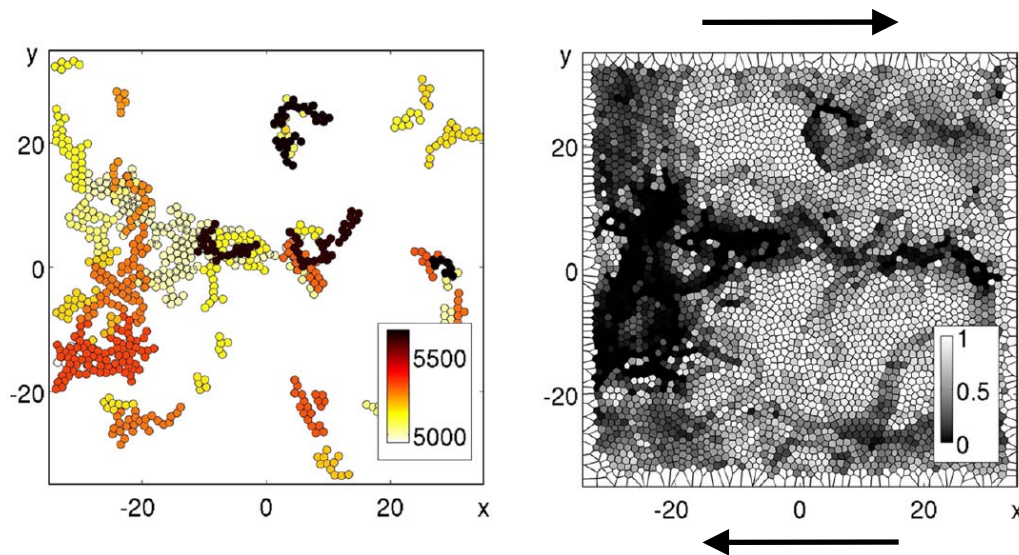


Acknowledgement:  
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N. V. Priezjev, “Heterogeneous relaxation dynamics in amorphous materials under cyclic loading”, *Phys. Rev. E* **87**, 052302 (2013). Preprint: <http://xxx.lanl.gov/abs/1301.1666>

# Dynamical Heterogeneities in Granular Media and Supercooled Liquids

## • Cyclic Shear Experiment on Dense 2D Granular Media



Spatial location of successive clusters of cage jumps

Power-law distribution of clusters sizes

Candelier, Dauchot, and Biroli, *PRL* **102**, 088001 (2009).

## • Fluidized Bed Experiment: Monolayer of Bidisperse Beads

Candelier, Dauchot, and Biroli, *EPL* **92**, 24003 (2010).

## • 2D Softly Repulsing Particle Molecular Dynamics Simulation (Supercooled Liquids at Eqm)

Candelier, Widmer-Cooper, Kummerfeld, Dauchot, Biroli, Harrowell, Reichman, *PRL* (2010).

## Present study:

- 3D metallic glass under periodic strain?
- Particle diffusion depends on the strain amplitude
- Structural relaxation and dynamical heterogeneities
- Particle hopping dynamics clusters of mobile particles
- Dynamical facilitation of mobile particles

## Details of molecular dynamics simulations and parameter values

Binary 3D Lennard-Jones Kob-Andersen mixture:

$$V_{LJ}(r) = 4\varepsilon_{\alpha\beta} \left[ \left( \frac{\sigma_{\alpha\beta}}{r} \right)^{12} - \left( \frac{\sigma_{\alpha\beta}}{r} \right)^6 \right]$$

Interaction parameters for  $\alpha\beta = A$  and  $B$  particles:

$$\varepsilon_{AA} = 1.0, \varepsilon_{AB} = 1.5, \varepsilon_{BB} = 0.5, m_A = m_B, N_p = 2940$$

$$\sigma_{AA} = 1.0, \sigma_{AB} = 0.8, \sigma_{BB} = 0.88, \tau = \sigma_{AA} \sqrt{m_A / \varepsilon_{AA}}$$

W. Kob and H. C. Andersen, *Phys. Rev. E* **51**, 4626 (1995).

$$\text{Monomer density: } \rho = \rho_A + \rho_B = 1.20 \sigma^{-3}$$

$$\text{Temperature: } T = 0.1 \varepsilon / k_B < T_g = 0.45 \varepsilon / k_B$$

$$\text{System dimensions: } 12.81 \sigma \times 14.79 \sigma \times 12.94 \sigma$$

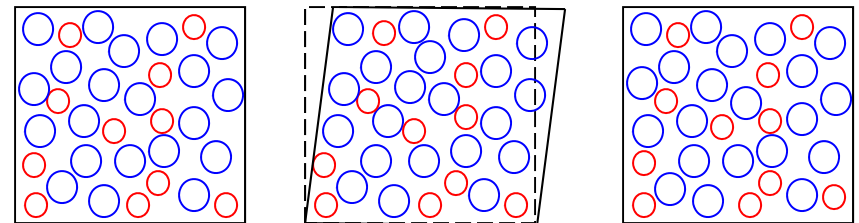
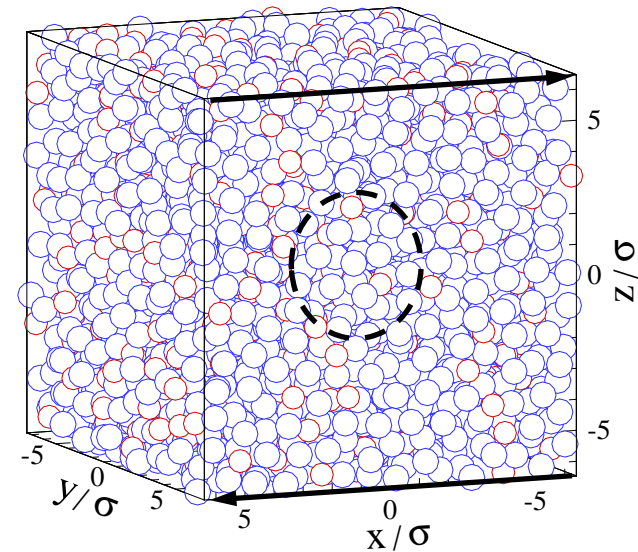
Lees-Edwards periodic boundary conditions

$$\text{The SLLOD equations of motion: } \Delta t_{MD} = 0.005 \tau$$

$$\text{Oscillatory shear strain: } \dot{\gamma}(t) = \dot{\gamma}_0 \cos(\omega t)$$

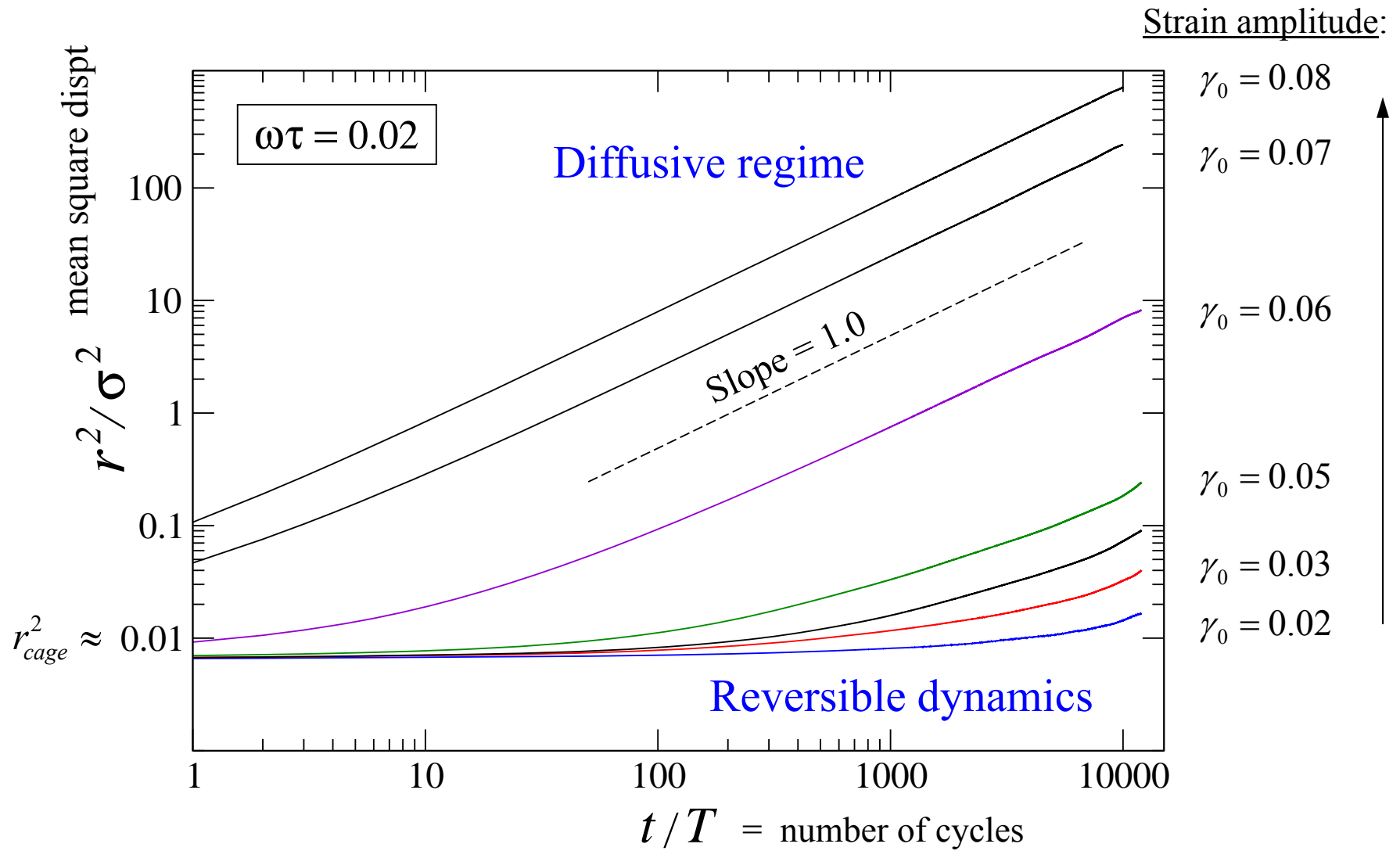
$$\text{Strain amplitude: } \gamma_0 = \dot{\gamma}_0 / \omega, \quad \omega = 0.02 \tau^{-1}$$

$$\text{Oscillation period: } T = 2\pi / \omega = 314.16 \tau$$

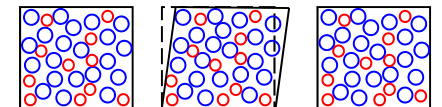


12,000 cycles ( $\approx 7.5 \times 10^8$  MD steps)

# Mean square displacement as a function of time for different strain amplitudes

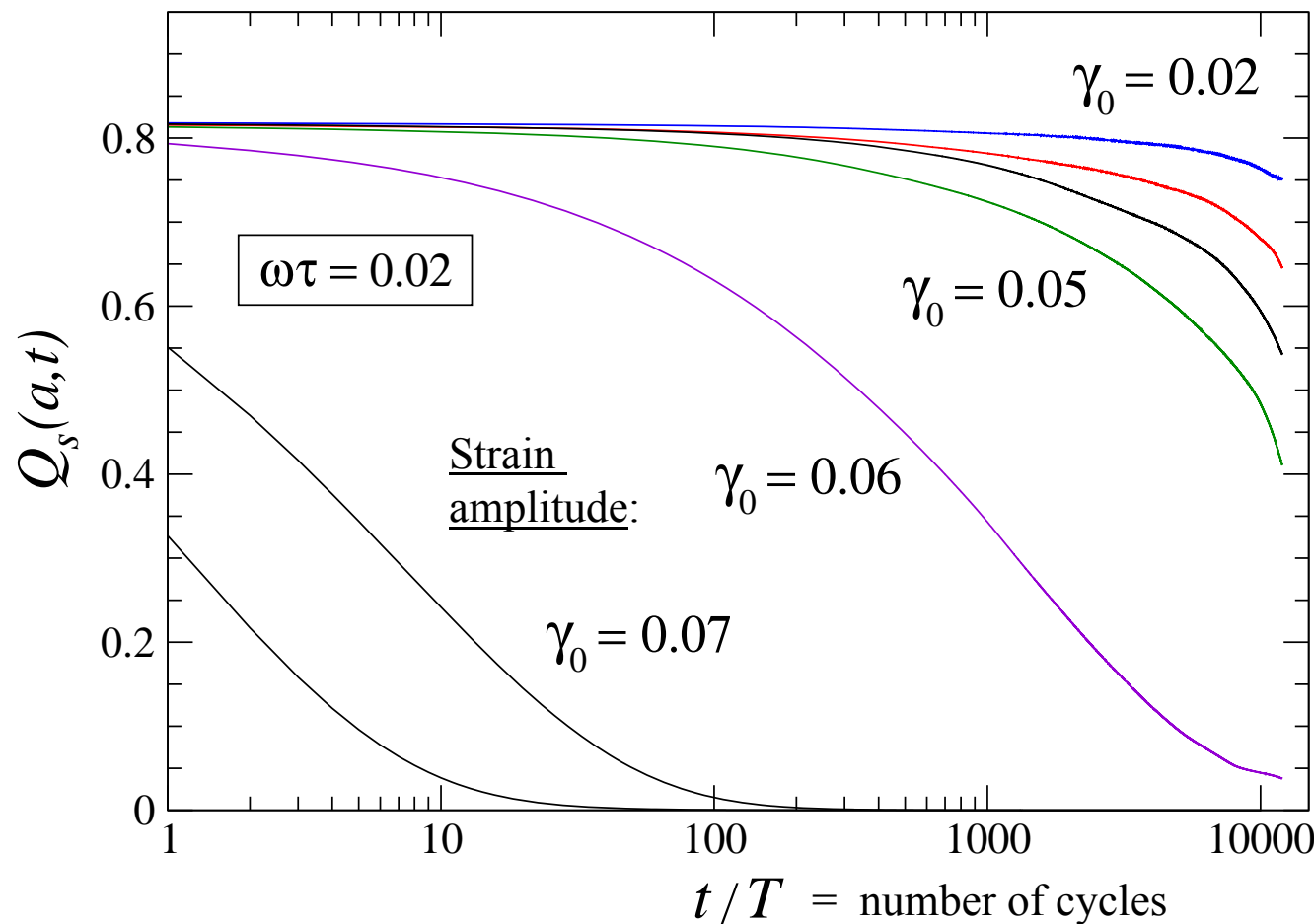


Oscillation period:  $T = 2\pi / \omega = 314.16 \tau$



## Self-overlap order parameter $Q_s(a, t)$ for different strain amplitudes

$$Q_s(a, t) = \frac{1}{N_p} \sum_{i=1}^{N_p} \exp\left(-\frac{\Delta r_i(t)^2}{2a^2}\right) \quad a = 0.12\sigma = \text{probed length scale} \sim \text{max in } X_4(a, t)$$



$Q_s(a, t)$  describes structural relaxation of the material.  
 Measure of the spatial overlap between particles positions.

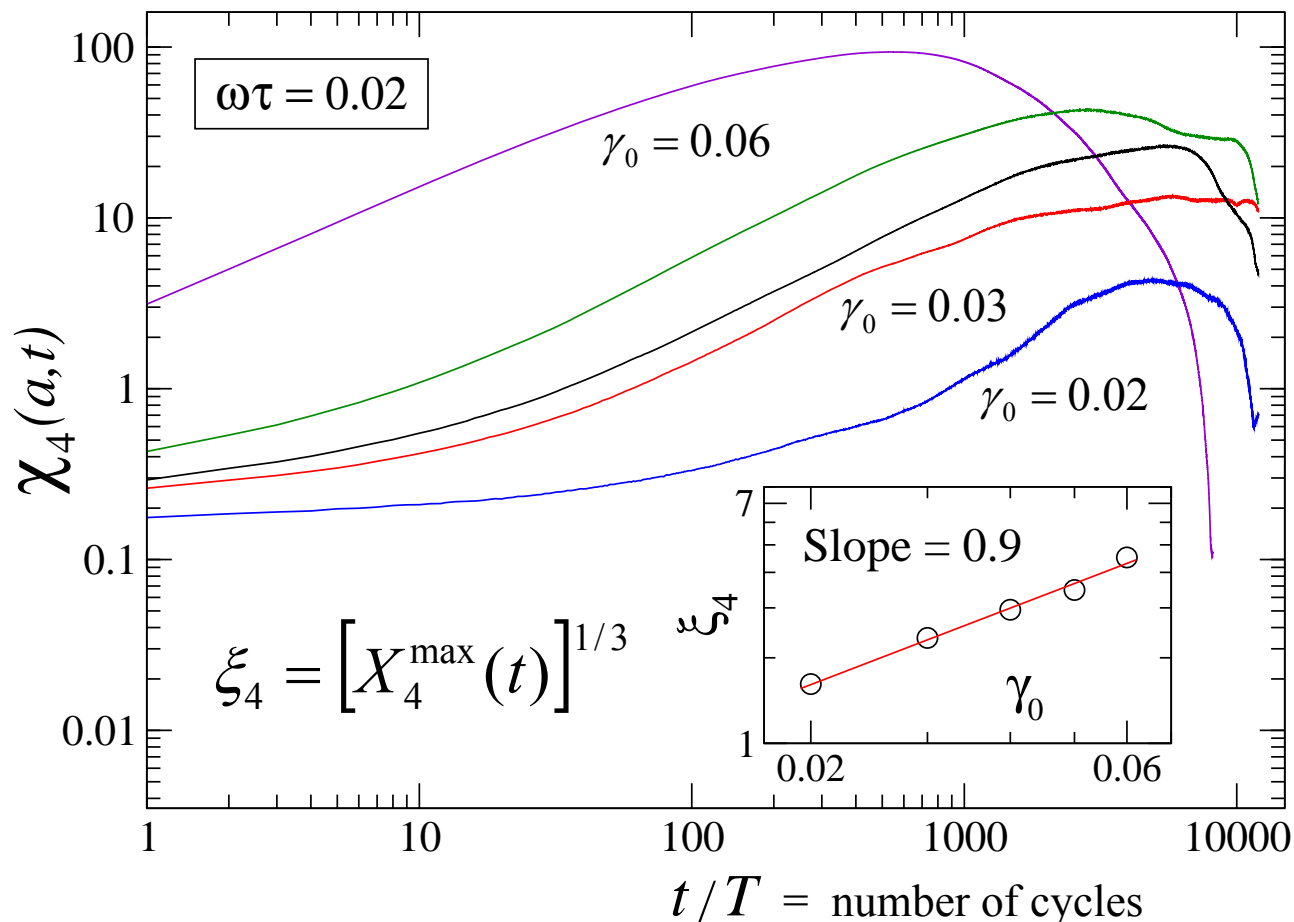
Reversible dynamics:  
 $Q_s(t) \approx \text{constant}$

Diffusive regime:  
 $Q_s(t)$  vanishes at large  $t$

Susceptibility  
 $X_4(a, t) = ?$

## Dynamical susceptibility as a function of time for different strain amplitudes

$$X_4(a, t) = N_p \left( \langle Q_s(a, t)^2 \rangle - \langle Q_s(a, t) \rangle^2 \right) \quad a = 0.12\sigma = \text{probed length scale} \sim \text{max in } X_4(a, t)$$



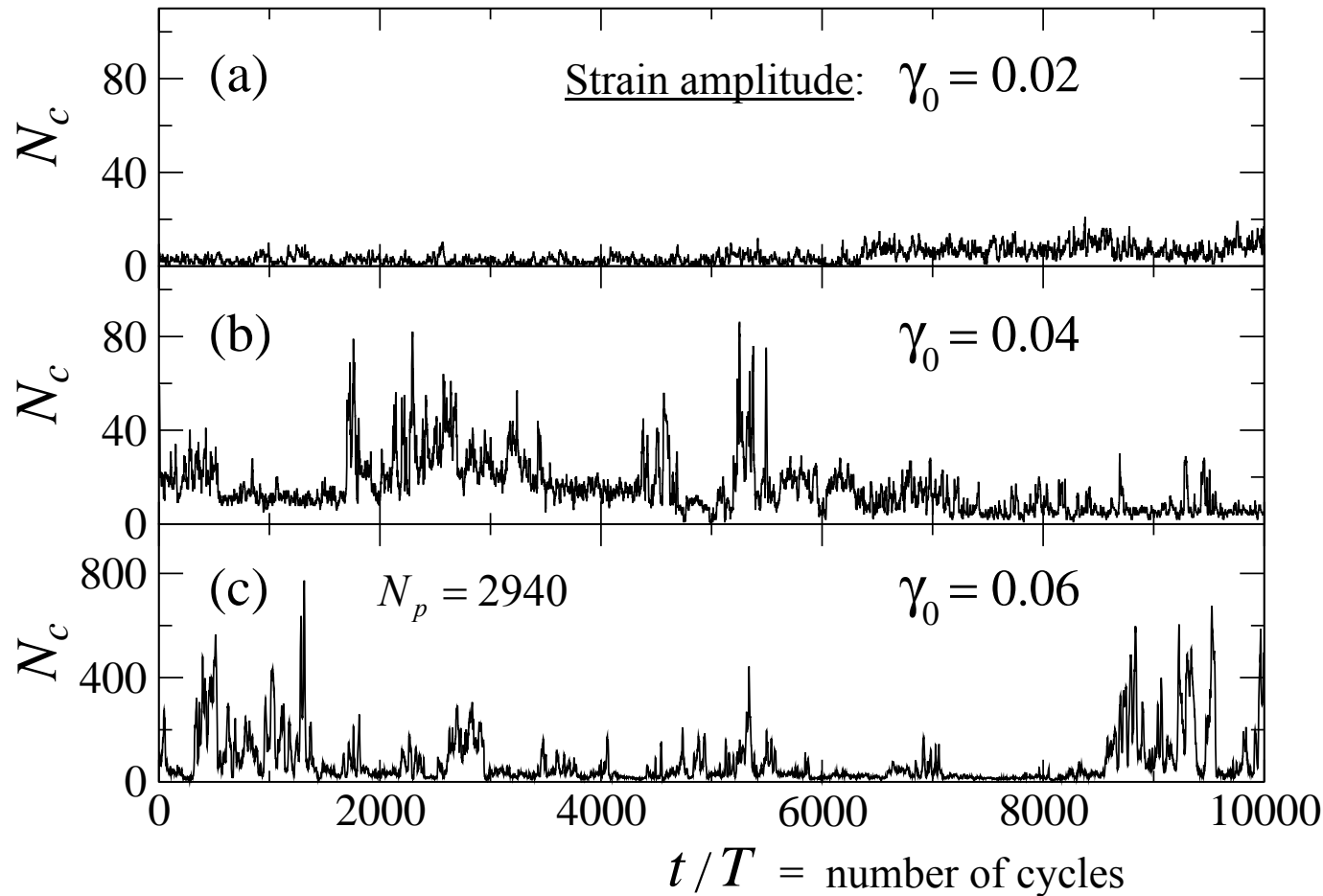
$X_4(a, t)$  is dynamical susceptibility, which is the variance of  $Q_s$ .

Maximum  $X_4(a, t)$  indicates the largest spatial correlation between localized particles.

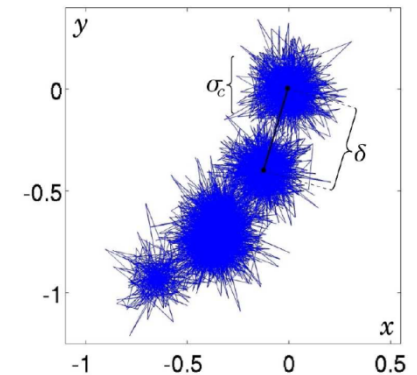
Berthier & Biroli (2011)

The dynamic correlation length increases with increasing strain amplitude (in contrast to steadily sheared supercooled liquids and glasses).

Number of particles undergoing cage jumps  $N_c$  as a function of time  $t/T$



Numerical algorithm for detection of cage jumps:



Candelier, Dauchot, Biroli, *PRL* (2009).

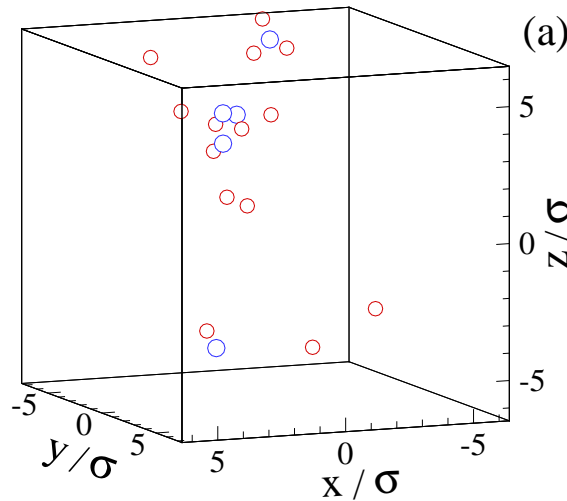
Periodic deformation = intermittent bursts of large particle displacements.

Power spectrum  $\sim \text{frequency}^{-2}$  = simple **Brownian** noise

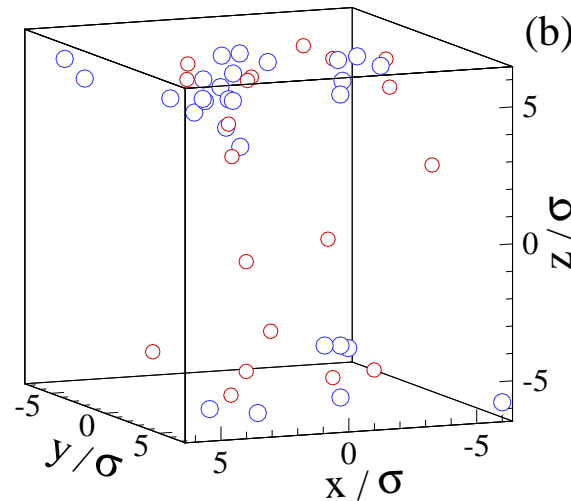
Scale-invariant processes or **Pink** noise = "1/f noise"

# Typical clusters of mobile particles A (blue circles) and B (red circles)

$\gamma_0 = 0.02$   
Single particle  
reversible jumps:



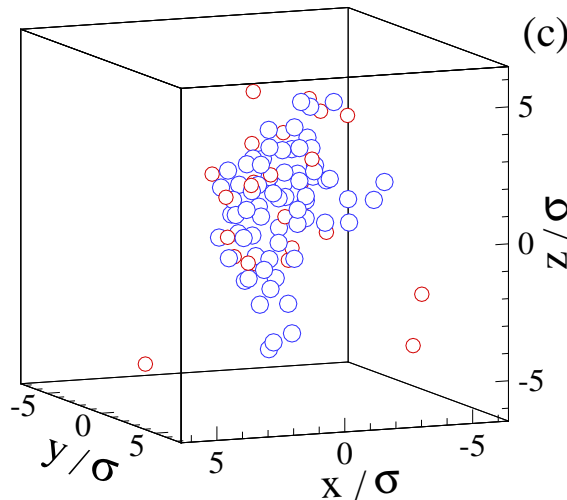
(a)



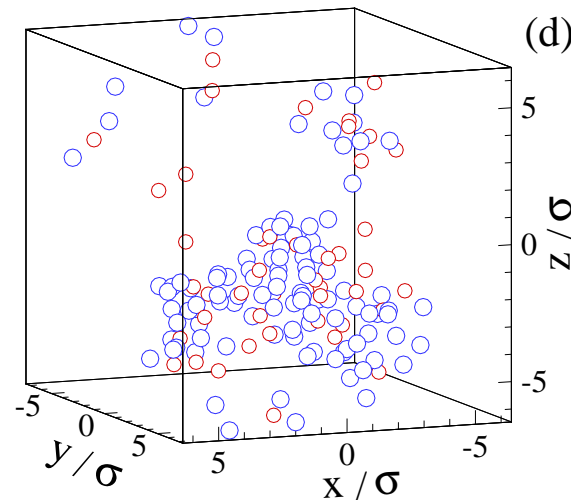
(b)

Strain amplitude:  
 $\gamma_0 = 0.03$

$\gamma_0 = 0.04$   
Compact clusters;  
Irreversible jumps:



(c)



(d)

Strain amplitude:  
 $\gamma_0 = 0.05$   
 $\gamma_0 \geq 0.06$

$$\xi_4 = \gamma_0^{0.9}$$

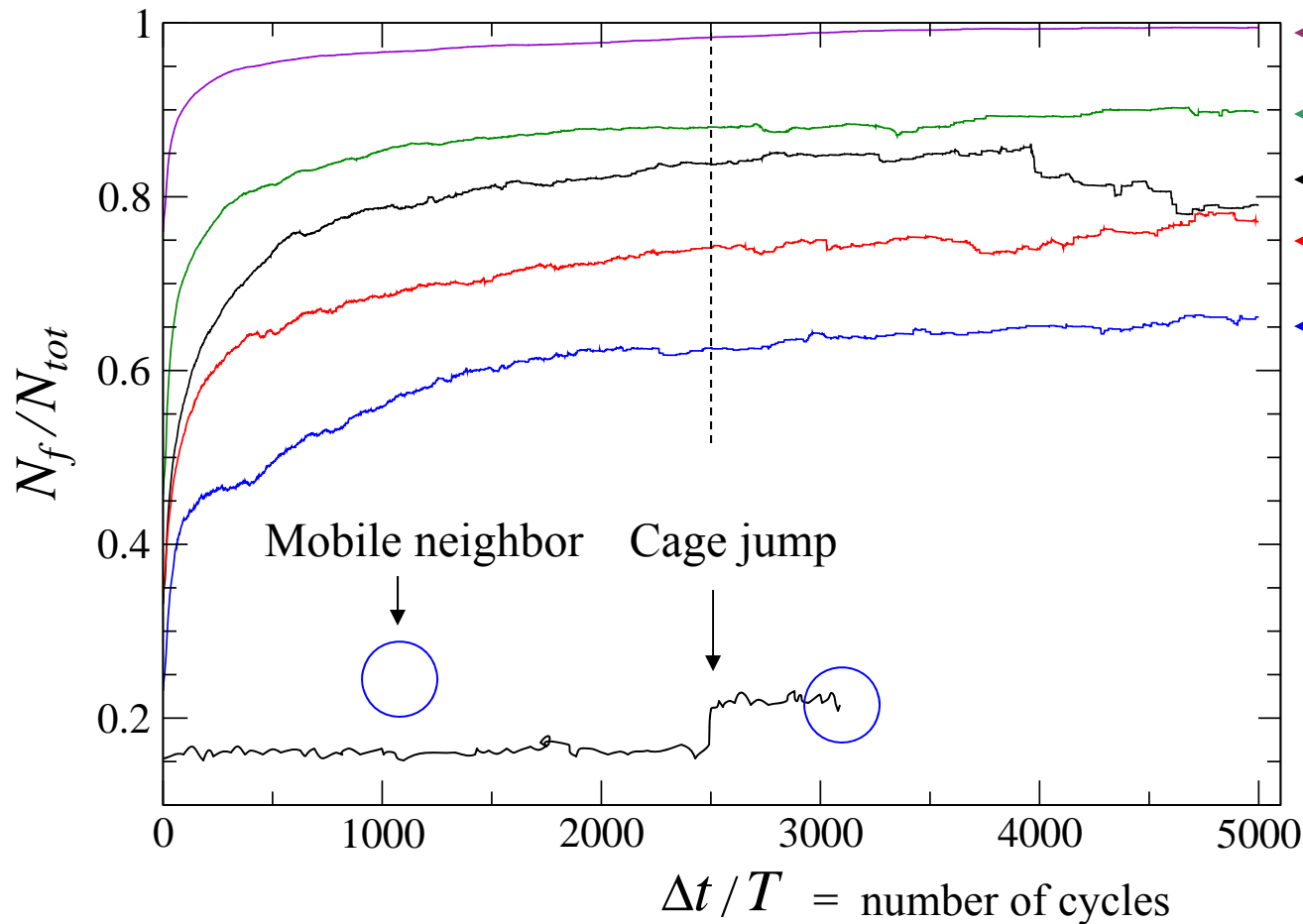
The system is  
fully relaxed over  
about  $10^4$  cycles



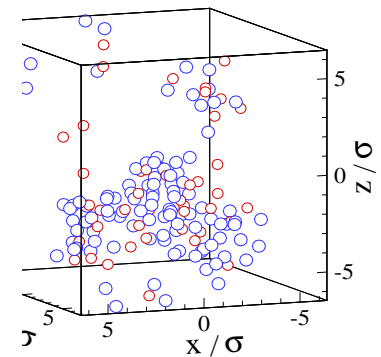
# Fraction of dynamically facilitated particles increases with strain amplitude

$\Delta t$  = time interval when a particles is immobile (inside the cage)

Strain amplitude:



- ←  $\gamma_0 = 0.06$
- ←  $\gamma_0 = 0.05$
- ←  $\gamma_0 = 0.04$
- ←  $\gamma_0 = 0.03$
- ←  $\gamma_0 = 0.02$

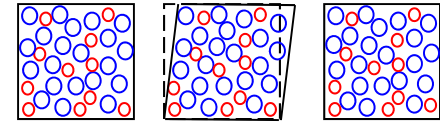


Large surface area = high probability to have mobile neighbors.

Oscillation period:  $T = 2\pi / \omega = 314.16 \tau$

Vogel and Glotzer, *Phys. Rev. Lett.* **92**, 255901 (2004).

## Important conclusions:



- MD simulations of the binary 3D Lennard-Jones Kob-Andersen mixture at  $T = 0.1 \varepsilon/k_B$  under spatially homogeneous, time-periodic shear strain.
- At small strain amplitudes, the mean square displacement exhibits a broad sub-diffusive plateau and the system undergoes nearly reversible deformation over about  $10^4$  cycles.
- At larger strain amplitudes, the transition to the diffusive regime occurs at shorter time intervals and the relaxation process involves intermittent bursts of large particle displacements.
- The detailed analysis of particle hopping dynamics and the dynamic susceptibility  $X_4(a, t)$  indicates that mobile particles aggregate into clusters whose sizes increase at larger strain amplitudes. (In contrast to sheared supercooled liquids and glasses).  $\xi_4 = \gamma_0^{0.9}$
- Fraction of dynamically facilitated mobile particles increases at larger strain amplitudes.

N. V. Priezjev, “Heterogeneous relaxation dynamics in amorphous materials under cyclic loading”, *Phys. Rev. E* **87**, 052302 (2013). Preprint: <http://xxx.lanl.gov/abs/1301.1666>