

5-Card Trick

To my accomplice for the “5-Card Trick”. In this trick, I’ll put 5 cards on the table in the shape of a “T”, always with the bottom card face down as in the following 2 examples. For the 3 cards in the top row, let each face-down card be a “0” and each face-up card be a “1”, then you get a 3-digit binary number. Here are two examples illustrating this and the rest of the trick.

Example 1. Solution: the top row gives the binary number 3, count up 3 cards from the next card, and that gives the hidden card to be the 8 of Hearts.

$$\begin{array}{ccc}
 \boxed{??} & \boxed{2\clubsuit} & \boxed{7\diamond} & \equiv 011 \equiv 3 \\
 & \boxed{5\heartsuit} & & \boxed{6\heartsuit}, \boxed{7\heartsuit}, \boxed{8\heartsuit} \\
 & \boxed{??} & & \equiv \boxed{8\heartsuit}
 \end{array}$$

Example 2. Suppose the five cards are as follows.

$$\begin{array}{ccc}
 \boxed{3\clubsuit} & \boxed{??} & \boxed{K\diamond} & \equiv 101 \equiv 5 \\
 & \boxed{Q\spadesuit} & & \boxed{K\spadesuit}, \boxed{A\spadesuit}, \boxed{2\spadesuit}, \boxed{3\spadesuit}, \boxed{4\spadesuit} \\
 & \boxed{??} & & \equiv \boxed{4\spadesuit}
 \end{array}$$

Solution: the top row gives the binary number 5, count up 5 cards from the next card, and that gives the hidden card to be the 4 of Spades. **Note here how we count “up” from ace to 2”.**

For your information, here are the binary numbers from 1 to 7.

Binary Number	001	010	011	100	101	110	111
Decimal Number	1	2	3	4	5	6	7

Question for the audience: Why can you always do this?